

# An Efficient and Secure Smart Card Based Password Authentication Scheme

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## Abstract

With the advancement of internet network technologies, remote user authentication schemes using smart cards have been widely adopted. In order to satisfy the requirements of a remote user authentication scheme, the smart card has become an essential device, one that is widely used because of its low computational cost and expedient portability. Recently, Li et al. pointed out some security weaknesses in Chen et al.'s scheme, such as forward secrecy and the wrong password login problem, and proposed an enhanced user password authentication scheme based on smart card. However, we found weaknesses in their scheme. Accordingly, we propose an enhanced scheme to remedy these security weaknesses, and prove that our scheme is more secure and efficient for network application with several positive properties.

*Keywords:* Authentication, hash function, security, smart card

## 1 Introduction

With the development of Internet network technologies, remote user authentication schemes using smart cards have been widely adopted. It is generally known that the first proposed remote authentication scheme was based on a password to identify a legitimate user even over an insecure channel [1, 12, 19]. This is the subject of a published research by Lamport in 1981 [8]. It has been claimed that there is a potential security threat caused by a stored verifier table on a remote authentication system, because the verifier table risks being modified by an adversary and has a high maintenance cost, even though all secret passwords can be encrypted against the threat of disclosure. Later, Hwang and Li [4] presented the weakness of Lamport's scheme and proposed a new scheme based on the ElGamal public-key encryption system [3] to solve

the corresponding problem. In this novel method, there is no need to maintain a verifier table to achieve remote user authentication. In view of the low cost and capacity of cryptosystems, Sun [18] developed an authentication scheme to enhance the performance efficiency of Hwang and Li's scheme by involving several one-way hash operations, such that the scheme could serve as an ideal substitute for high-cost modular exponentiations. Nevertheless, these two mentioned schemes could not provide users with a free choice of passwords and mutual authentication.

Since a smart card has tamper-resistant properties, it can solve the problem of maintaining the verifier table on the server side. In a smart card based authentication system, only the user is required to hold a smart card, which was issued by the server for more convenient communication and which contained all kinds of stored secret information. Many related studies [5, 6, 7, 11, 16] have investigated smart cards and the smart card has become essential in remote authentication schemes. In 2009, Xu et al. [20] proposed a novel user authentication and claimed that their scheme is secure against various attacks. However, Song [14] and Sood et al. [15] found that Xu et al.'s scheme has some weaknesses and proposed improved schemes. Subsequently, Chen et al. [2] pointed out that there are vulnerabilities on Song and Sood et al.'s schemes. Then, Chen et al. presented an enhanced version to solve the weaknesses. Recently, Li et al. [9] claimed that Chen et al.'s scheme is still insecure and proposed a modified smart card based remote user password authentication scheme. Unfortunately, we find that there are weaknesses in Li et al.'s scheme, such as from a man-in-the-middle attack and an insider attack. Hence, we propose a novel scheme to defend against these security weaknesses. Furthermore, our proposed scheme has better computational efficiency, which has become clear by comparing our work with previous schemes. In addition, our scheme has the following properties:

- F1.** Mutual authentication: Both the legal user and the remote server can authenticate each other successfully.
- F2.** Session key agreement: The legal user and the remote server can negotiate a session key and utilize it to process subsequent communication.
- F3.** Freely chosen and exchanged password: A legal user can freely choose and change the password.
- F4.** Withstands a man-in-the-middle attack: Our scheme can withstand a man in the middle attack.
- F5.** Withstands an insider attack: No adversary can present an insider attack.
- F6.** Withstands a replay attack: No one can perform a replay attack.
- F7.** Perfect forward secrecy: Even if an adversary can obtain contiguous knowledge of the long-term key, the adversary cannot derive previous session keys.
- F8.** Satisfying known-key security: No one can utilize the secret information of a legal user to derive the session key.

The rest of this paper is organized as follows. In Section 2, we briefly review Li et al.'s smart-card-based password authentication scheme and Section 3 analyzes its weaknesses. In Section 4, we propose our scheme. Section 5 gives security and performance analyses of the proposed scheme. Finally, we present our conclusions in Section 6.

Table 1: The notations used in both Li et al.'s and our proposed schemes

$U_i$	The user $i$
$S$	The authentication server
$ID_i$	The identity of the user $U_i$
$PW_i$	The password of the user $U_i$
$x$	The master secret key of the server $S$
$T_i$	The timestamp of the user $U_i$
$T'_i$	The time of receiving the login request message
$T_s$	The timestamp of the server $S$
$T'_s$	The time of receiving the mutual authentication message
$\Delta T$	A valid time threshold
$h(\cdot)$	A collision-free one-way hash function
$\parallel$	The message concatenation operation
$\oplus$	The bitwise XOR operation
$sk$	The shared session key

## 2 Review of Li et al.'s Scheme

In this section, we briefly review Li et al.'s smart card based password authentication scheme [9] before demonstrating its weaknesses. Their scheme is an improvement of Chen et al.'s scheme [2] and the security depends on the hardness of solving the discrete logarithm problem [13].

The notations used in both Li et al.'s and our proposed schemes are listed in Table 1.

Their scheme involves two parties, i.e., the user  $U_i$  and the server  $S$ , to communicate with each other to perform the following four phases: (1) The registration phase; (2) the login phase; (3) the authentication phase; and (4) the password change phase. Since the security basis of their scheme is the discrete logarithm problem, the server  $S$  needs to initialize some parameters before the registration phase. The server  $S$  selects two large prime numbers  $p$  and  $q$  that satisfy  $p = 2q + 1$ , the master secret key  $x \in Z_q^*$  ( $Z_q$  denotes the ring of integers modulo  $q$  and  $Z_q^*$  denotes the multiplicative group of  $Z_q$ ), and a collision-free one-way hash function  $h(\cdot)$ . Then, the four phases are executed as follows and are illustrated in Figure 1.

### 2.1 Registration Phase

**Step 1.** The user  $U_i$  selects his/her identity  $ID_i$  and password  $PW_i$  and submits them to the server  $S$  for registration over a secure channel.

**Step 2.** The server  $S$  computes two parameters:  $A_i = h(ID_i \parallel PW_i)^{PW_i} \bmod p$  and  $B_i = h(ID_i)^{(x+PW_i)} \bmod p$ .

**Step 3.** The server  $S$  stores the data  $\{A_i, B_i, h(\cdot), p, q\}$  on a new smart card and issues the smart card to the user  $U_i$  over a secure channel.

### 2.2 Login Phase

**Step 1.** The user  $U_i$  inserts his/her smart card into a card reader and inputs his/her identity  $ID_i$  and password  $PW_i$ .

**Step 2.** The smart card computes  $A_i^* = h(ID_i \parallel PW_i)^{PW_i} \bmod p$  and examines whether  $A_i^*$  is equal to  $A_i$ . If the equation holds, the smart card continues to perform Step 3; otherwise, the smart card terminates this session.

**Step 3.** The smart card randomly selects a number  $\alpha \in R_{Z_q^*}$  and computes the following parameters:

$$\begin{aligned} C_i &= B_i / h(ID_i)^{PW_i} \bmod p, \\ D_i &= h(ID_i)^\alpha \bmod p, \\ M_i &= h(ID_i \parallel C_i \parallel D_i \parallel T_i), \end{aligned}$$

where  $T_i$  is the current timestamp of the user  $U_i$ .

**Step 4.** The smart card sends the login request message  $\{ID_i, D_i, M_i, T_i\}$  to the server  $S$ .

### 2.3 Authentication Phase

**Step 1.** The server  $S$  verifies whether  $ID_i$  is valid and  $T'_i - T_i \leq \Delta T$ , where  $T'_i$  is the time of receiving the login request message and  $\Delta T$  is a valid time threshold. If both conditions are true, the server  $S$

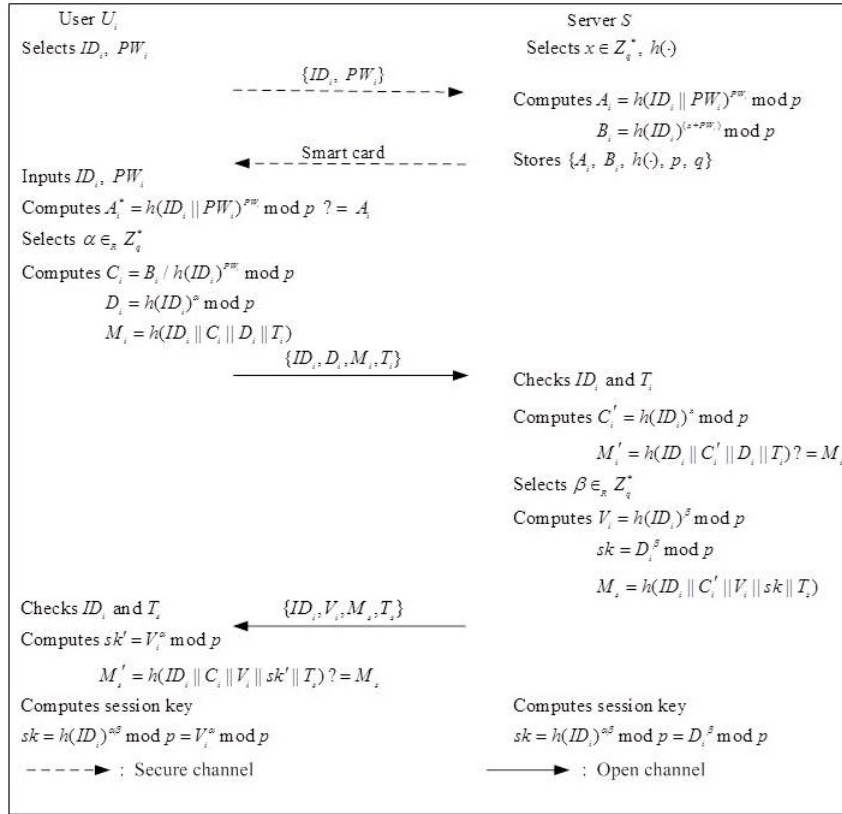


Figure 1: Li et al.'s scheme

continues to execute Step 2; otherwise, the server  $S$  rejects the login request.

**Step 2.** The server  $S$  computes two parameters:  $C_i' = h(ID_i)^x \bmod p$  and  $M_i' = h(ID_i \parallel C_i' \parallel D_i \parallel T_i)$ . Then, the server  $S$  compares whether  $M_i'$  equals  $M_i$ . If they are equal, the server  $S$  confirms that the user  $U_i$  is valid and the login request is accepted; otherwise, the login request is rejected.

**Step 3.** The server  $S$  randomly selects a number  $\beta \in_R Z_q^*$  and computes the following parameters:

$$\begin{aligned} V_i &= h(ID_i)^\beta \bmod p, \\ sk &= D_i^\beta \bmod p, \\ M_s &= h(ID_i \parallel C_i' \parallel V_i \parallel sk \parallel T_s), \end{aligned}$$

where  $T_s$  is the current timestamp of the server  $S$ .

**Step 4.** The server  $S$  sends the mutual authentication message  $\{ID_i, V_i, M_s, T_s\}$  to the user  $U_i$ .

**Step 5.** Upon receiving the message  $\{ID_i, V_i, M_s, T_s\}$ , the user  $U_i$  checks the validity of  $ID_i$  and whether  $T_s' - T_s \leq \Delta T$ , where  $T_s'$  is the time of receiving the mutual authentication message. If both of them hold, the user  $U_i$  continues to perform Step 6; otherwise, the user  $U_i$  terminates this connection.

**Step 6.** The user  $U_i$  computes two parameters:  $sk' = V_i^\alpha \bmod p$  and  $M_s' = h(ID_i \parallel C_i' \parallel V_i \parallel sk' \parallel T_s)$ . Then, the user  $U_i$  checks whether  $M_s'$  equals  $M_s$ . If they are equal, the validity of the server  $S$  is authenticated; otherwise, the session is terminated.

**Step 7.** The user  $U_i$  and the server  $S$  construct a shared session key  $sk = h(ID_i)^{\alpha\beta} \bmod p$  to ensure the secret communication.

## 2.4 Password Change Phase

**Step 1.** The user  $U_i$  inserts his/her smart card into a card reader, enters his/her old identity  $ID_i$  and password  $PW_i$ , and requests to change the password.

**Step 2.** The smart card computes  $A_i^* = h(ID_i \parallel PW_i)^{PW_i} \bmod p$  and checks whether  $A_i^*$  equals  $A_i$  that is stored in the smart card. If the equation holds, the user  $U_i$  submits the new password  $PW_i^{new}$ ; otherwise, the smart card rejects the password change request.

**Step 3.** The smart card computes  $A_i^{new} = h(ID_i \parallel PW_i^{new})^{PW_i^{new}} \bmod p$  and  $B_i^{new} = B_i \cdot h(ID_i)^{PW_i^{new}} / h(ID_i)^{PW_i} \bmod p$ . Then, the smart card replaces  $A_i$  and  $B_i$  with  $A_i^{new}$  and  $B_i^{new}$ , respectively.

### 3 Weaknesses of Li et al.'s Scheme

Li et al.'s scheme [9] can correct the design flaws of Chen et al.'s scheme [2], such as by ensuring perfect forward secrecy, quickly detecting the wrong password via the smart card without interacting with the server in the login phase, and provides a friendly and efficient password change. Additionally, Li et al. claimed that their scheme is very secure and can resist various types of attacks. We found, however, that Li et al.'s scheme cannot withstand a man-in-the-middle attack or an insider attack. In addition, the use of modulus exponential operations incurs a considerable computational cost. The details of these weaknesses are discussed below.

#### 3.1 Man-in-the-middle Attack

Li et al.'s scheme is vulnerable to a man-in-the-middle attack. Suppose that there exists an attacker  $U_E$  between the user  $U_i$  and the server  $S$ . The attacker  $U_E$  can intercept the login request message and the mutual authentication message transmitted between the user  $U_i$  and the server  $S$ , and then modify these messages.  $U_E$  can act as the user  $U_i$  to communicate with the server  $S$  and act as the server  $S$  to communicate with the user  $U_i$  without detection. This type of attack can be described as follows:

**Step 1.** In the login phase, the user  $U_i$ 's smart card sends the login request message  $\{ID_i, D_i, M_i, T_i\}$  to the server  $S$ . The attacker  $U_E$  intercepts this message.

**Step 2.** Since  $M_i = h(ID_i \parallel C_i \parallel D_i \parallel T_i)$ , the attacker  $U_E$  uses the intercepted values of  $ID_i, D_i, T_i$ , and  $M_i$  to guess  $C_i$ . Due to the fact that  $C_i = B_i/h(ID_i)^{PW_i} \bmod p = h(ID_i)^x \bmod p$  would remain the same in different sessions of the user  $U_i$  and the server  $S$ , the attacker  $U_E$  can easily determine the value of  $C_i$ .

**Step 3.** The attacker  $U_E$  generates  $D_E = h(ID_i)^e$  and computes  $M_E = h(ID_i \parallel C_i \parallel D_E \parallel T_E)$ . After that,  $U_E$  sends  $\{ID_i, D_E, M_E, T_E\}$  to the server  $S$ .

**Step 4.** The server  $S$  first checks the validity of  $ID_i$  and  $T_E$ , and then computes  $C'_i = h(ID_i)^x \bmod p$  and  $M'_E = h(ID_i \parallel C'_i \parallel D_E \parallel T_E)$ . Afterwards, the server  $S$  compares whether  $M'_E$  equals  $M_E$ . If they are equal, the server  $S$  believes that the attacker  $U_E$  is authenticated as the user  $U_i$ .

**Step 5.** The server  $S$  computes  $V_i = h(ID_i)^\beta \bmod p$ ,  $sk = D_E^\beta \bmod p = h(ID_i)^{e\beta} \bmod p$ , and  $M_s = h(ID_i \parallel C'_i \parallel V_i \parallel sk \parallel T_s)$ , then sends the mutual authentication message  $\{ID_i, V_i, M_s, T_s\}$  to the user  $U_i$ . The attacker  $U_E$  intercepts this message.

**Step 6.** The attacker  $U_E$  generates  $V_E = h(ID_i)^e$ ,  $sk_E = V_E \cdot D_i = h(ID_i)^{e\alpha} \bmod p$  and  $M''_E = h(ID_i \parallel C'_i \parallel V_E \parallel sk_E \parallel T'_E)$ . After that,  $U_E$  sends  $\{ID_i, V_E, M''_E, T'_E\}$  to the user  $U_i$ .

**Step 7.** The user  $U_i$  first checks the validity of  $ID_i$  and  $T'_E$ , and then computes  $sk' = V_E^\alpha \bmod p = h(ID_i)^{e\alpha} \bmod p$  and  $M'''_E = h(ID_i \parallel C_i \parallel V_E \parallel sk' \parallel T'_E)$ . Afterwards, the user  $U_i$  checks whether  $M'''_E$  equals  $M''_E$ . If they are equal, the user  $U_i$  believes that the attacker  $U_E$  is authenticated as the server  $S$ .

After performing the authentication phase, the user  $U_i$  believes that the attacker  $U_E$  is the server  $S$  and the server  $S$  believes that the attacker  $U_E$  is the user  $U_i$ . Moreover, user  $U_i$  and the server  $S$  trust that they have established a common session key. However, server  $S$  and the attacker  $U_E$  share a session key  $sk = h(ID_i)^{e\beta} \bmod p$ ; and user  $U_i$  and the attacker  $U_E$  share another session key  $sk' = h(ID_i)^{e\alpha} \bmod p$ . Consequently, Li et al.'s scheme cannot prevent a man-in-the-middle attack.

#### 3.2 Insider Attack

If server  $S$  directly obtains user  $U_i$ 's password  $PW_i$ , an insider attack takes place when an intruder steals  $PW_i$  from  $S$ . In Li et al.'s scheme, the user  $U_i$  selects their password  $PW_i$  and submits it to the server  $S$  for registration over a secure channel. Therefore, server  $S$  can obtain the user  $U_i$ 's password  $PW_i$  and cannot withstand an insider attack.

#### 3.3 Computational Inefficiency

From Li et al.'s scheme, we can see that it uses too many modulus exponential operations, which can incur unnecessary overhead. The computational cost in the login and authenticated phases are  $3E + 1M + 3H$  and  $4E + 4H$ , respectively, where  $E$  is modulus exponential operations,  $M$  is multiplication/division operations, and  $H$  is hashing operations. Li et al. claimed that although their scheme requires a higher computational cost, it can achieve higher security and usability compared with other related schemes. Unfortunately, this is not true according to the discussion in Subsections 3.1 and 3.2. In fact, the modulus exponential operations can be replaced with other appropriate operations to reduce the computational cost.

## 4 Our Proposed Scheme

To overcome the aforementioned weaknesses, we propose a novel smart card based password authentication scheme, which is secure and more efficient. By using the combination of collision-free one-way hash functions, bitwise XOR ( $\oplus$ ) and concatenation ( $\parallel$ ) operations instead of modulus exponential operations, our proposed scheme can significantly enhance computational efficiency while satisfying various security requirements. Our proposed scheme consists of four phases: (1) The registration phase; (2) the login phase; (3) the authentication phase; and (4) the

password change phase. In the following, we will describe the proposed scheme in detail.

### 4.1 Registration Phase

At the beginning of our proposed scheme, the server  $S$  selects the master secret key  $x$  and a collision-free one-way hash function  $h(\cdot)$ . Then, the user  $U_i$  registers to the server  $S$  by the way below:

**Step 1.** The user  $U_i$  first selects his/her identity  $ID_i$ , password  $PW_i$ , and a random number  $r$ , and then computes  $h(r \parallel PW_i)$ .  $U_i$  submits  $\{ID_i, h(r \parallel PW_i)\}$  to the server  $S$  for registration over a secure channel.

**Step 2.** The server  $S$  computes the following parameters:

$$\begin{aligned} A_i &= h(ID_i \oplus x) \parallel h(x), \\ B_i &= A_i \oplus h(r \parallel PW_i), \\ C_i &= h(A_i \parallel ID_i \parallel h(r \parallel PW_i)). \end{aligned}$$

**Step 3.** The server  $S$  stores the data  $\{B_i, C_i, h(\cdot)\}$  on a new smart card and issues the smart card to the user  $U_i$  over a secure channel.

**Step 4.** The user  $U_i$  stores the random number  $r$  into the smart card.

The registration phase is depicted in Figure 2.

### 4.2 Login Phase

This phase is invoked whenever the user  $U_i$  wants to login to the server  $S$ . The steps of this phase are conducted as follows:

**Step 1.** The user  $U_i$  inserts his/her smart card into a card reader and inputs his/her identity  $ID_i$  and password  $PW_i$ .

**Step 2.** The smart card first computes two parameters:  $A'_i = B_i \oplus h(r \parallel PW_i)$  and  $C'_i = h(A'_i \parallel ID_i \parallel h(r \parallel PW_i))$ . Then, the smart card examines whether  $C'_i$  is equal to  $C_i$ . If the equation holds, the smart card continues to perform Step 3; otherwise, the smart card terminates this session.

**Step 3.** The smart card randomly selects a number  $\alpha$  and computes the following parameters:

$$\begin{aligned} D_i &= h(ID_i \oplus \alpha), \\ E_i &= A'_i \oplus \alpha \oplus T_i, \end{aligned}$$

where  $T$  is the current timestamp of the user  $U_i$ .

**Step 4.** The smart card sends the login request message  $\{ID_i, D_i, E_i, T_i\}$  to the server  $S$ .

### 4.3 Authentication Phase

After completing this phase, the user  $U_i$  and the server  $S$  can mutually authenticate each other and establish a shared session key for the subsequent secret communication. The steps of this phase are shown as follows:

**Step 1.** The server  $S$  verifies whether  $ID_i$  is valid and  $T'_i - T_i \leq \Delta T$ , where  $T'_i$  is the time of receiving the login request message and  $\Delta T$  is a valid time threshold. If both conditions are true, the server  $S$  continues to execute Step 2; otherwise, the server  $S$  rejects the login request.

**Step 2.** The server  $S$  computes the following parameters:

$$\begin{aligned} A_i &= h(ID_i \oplus x) \parallel h(x), \\ \alpha' &= E_i \oplus A_i \oplus T_i, \\ D'_i &= h(ID_i \oplus \alpha'). \end{aligned}$$

Then, the server  $S$  compares whether  $D'_i$  equals  $D_i$ . If they are equal, the server  $S$  confirms that the user  $U_i$  is valid and the login request is accepted; otherwise, the login request is rejected.

**Step 3.** The server  $S$  randomly selects a number  $\beta$  and computes the following parameters:

$$\begin{aligned} F_i &= h(ID_i \oplus \beta), \\ G_i &= A_i \oplus \beta \oplus T_s, \end{aligned}$$

where  $T_s$  is the current timestamp of the server  $S$ .

**Step 4.** The server  $S$  sends the mutual authentication message  $\{F_i, G_i, T_s\}$  to the user  $U_i$ .

**Step 5.** Upon receiving the message  $\{F_i, G_i, T_s\}$ , the user  $U_i$  checks the validity of  $T_s$ . If  $T'_s - T_s \leq \Delta T$ , where  $T'_s$  is the time of receiving the mutual authentication message, the user  $U_i$  continues to perform Step 6; otherwise, the user  $U_i$  terminates this connection.

**Step 6.** The user  $U_i$  computes  $\beta' = G_i \oplus A'_i \oplus T_s$  and  $F'_i = h(ID_i \oplus \beta')$ , and then checks whether  $F'_i$  equals  $F_i$ . If they are equal, the validity of the server  $S$  is authenticated; otherwise, the session is terminated.

**Step 7.** The user  $U_i$  and the server  $S$  construct a shared session key  $sk = h(\alpha \parallel \beta' \parallel h(A'_i \oplus ID_i)) = h(\alpha' \parallel \beta \parallel h(A_i \oplus ID_i))$  to ensure the secret communication.

The login and authentication phases are shown in Figure 3.

### 4.4 Password Change Phase

**Step 1.** The user  $U_i$  inserts his/her smart card into a card reader, enters his/her old identity  $ID_i$  and password  $PW_i$ , and requests to change the password.



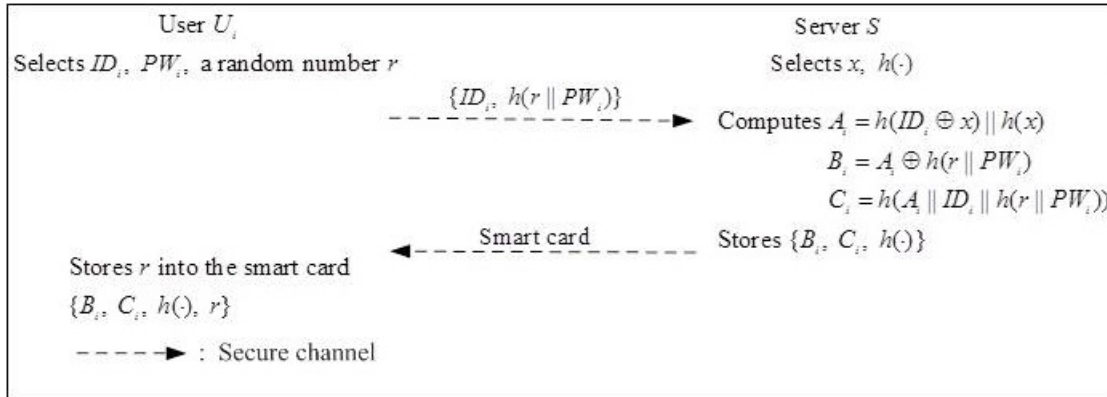


Figure 2: Registration phase of our proposed scheme

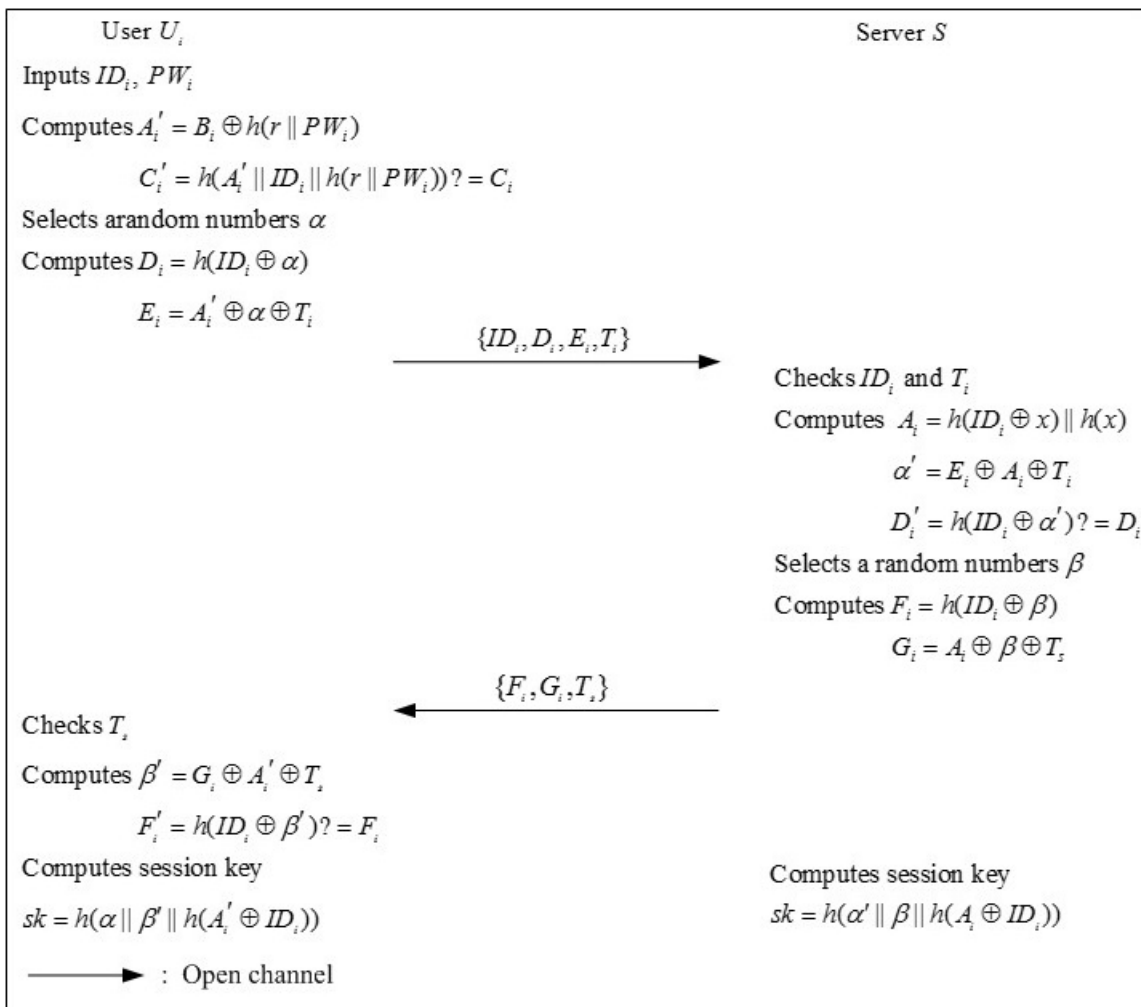


Figure 3: Login and authentication phases of our proposed scheme

**Step 2.** The smart card computes  $A_i^* = B_i \oplus h(r \parallel PW_i)$  and  $C_i^* = h(A_i^* \parallel ID_i \parallel h(r \parallel PW_i))$ , and then checks whether  $C_i^*$  equals  $C_i$  that is stored in the smart card. If the equation holds, the user  $U_i$  submits the new password  $PW_i^{new}$ ; otherwise, the smart card rejects the password change request.

**Step 3.** The smart card computes  $B_i^{new} = A_i^* \oplus h(r \parallel PW_i^{new})$  and  $C_i^{new} = h(A_i^* \parallel ID_i \parallel h(r \parallel PW_i^{new}))$ . Then, the smart card replaces  $B_i$  and  $C_i$  with  $B_i^{new}$  and  $C_i^{new}$ , respectively.

## 5 Analysis of the Proposed Scheme

In this section, we analyze the security and performance of our proposed scheme and make comparisons with other related works.

### 5.1 Functionality and Security Analyses

#### 5.1.1 Mutual Authentication

Our proposed scheme can achieve mutual authentication such that the user and the server can successfully verify the validity of each other. In Step 2 of the authentication phase, the server  $S$  computes  $D_i' = h(ID_i \oplus \alpha')$ , and then compares whether  $D_i'$  equals  $D_i$  that was sent by the user  $U_i$ . If they are equal, the server  $S$  confirms that user  $U_i$  is valid. On the other hand, in Step 6 of the authentication phase, user  $U_i$  computes  $F_i' = h(ID_i \oplus \beta')$ , and then checks whether  $F_i'$  equals  $F_i$  that was sent by the server  $S$ . If they are equal, the validity of the server  $S$  is authenticated.

#### 5.1.2 Session Key Agreement

After achieving mutual authentication, the user and the server must negotiate a common session key, which is used to encrypt the data transmitted between the user and the server in the subsequent confidential communications. In our proposed scheme, the user and the server share the session key  $sk = h(\alpha \parallel \beta' \parallel h(A_i' \oplus ID_i)) = h(\alpha' \parallel \beta \parallel h(A_i \oplus ID_i))$  at the end of the authentication phase.

#### 5.1.3 Freely Chosen and Exchanged Password

Our proposed scheme allows each user to choose their password in the registration phase so that users can easily remember their passwords. In addition, each user can change their password in the password change phase. If user  $U_i$  wants to update their password, the smart card checks the validity of the old password by comparing whether  $C_i^*$  equals  $C_i$ . If so, user  $U_i$  submits the new password  $PW_i^{new}$ . The smart card uses  $PW_i^{new}$  to compute  $B_i^{new}$  and  $C_i^{new}$ , and then replaces  $B_i$  and  $C_i$  with  $B_i^{new}$  and  $C_i^{new}$ , respectively. The password change phase is friendly and efficient since the smart card can complete

both the tasks of verification of old passwords and updating of new passwords. Thus, the user does not need to communicate with the server to change the password.

#### 5.1.4 Withstanding a Man-in-the-middle Attack

Assume that there exists an attacker  $U_E$  between the user  $U_i$  and the server  $S$ . In the login phase, the attacker  $U_E$  can intercept the login request message  $\{ID_i, D_i, E_i, T_i\}$  and attempts to forge it to act as user  $U_i$ . However,  $U_E$  cannot get  $A_i'$  and  $\alpha$  from the intercepted message. So, if  $U_E$  generates a fake  $E_i$  and sends it to the server  $S$ ,  $S$  can check that  $D_i'$  is not equal to the received  $D_i$  and concludes that  $U_E$  is not a valid user. On the other hand, the attacker  $U_E$  can intercept the mutual authentication message  $\{F_i, G_i, T_s\}$  and wants to forge it to act as the server  $S$ . Similarly, because  $U_E$  cannot obtain  $A_i$  and  $\beta$ , the user  $U_i$  will not be misled by the forged  $F_i'$  and concludes that  $U_E$  is not a valid server. Therefore, attacker  $U_E$  cannot modify the messages to pass the login and the authentication phases. This indicates that our proposed scheme can prevent a man-in-the-middle attack.

#### 5.1.5 Withstanding an Insider Attack

In the registration phase, the user conceals the password in a ciphertext from the server to resist an insider attack. More specifically, user  $U_i$  first selects their password  $PW_i$  and a random number  $r$ , and then submits  $h(r \parallel PW_i)$  to the server  $S$  for registration over a secure channel. As a result, server  $S$  cannot get the correct password  $PW_i$  and an insider attack will not occur.

#### 5.1.6 Withstanding Replay Attack

A replay attack means a malicious intruder repeats or delays valid transmitted messages without detection. Our proposed scheme can resist a replay attack by utilizing timestamps in the login and authentication phases. In Step 4 of the login phase, the smart card adds the timestamp  $T_i$  into the login request message  $\{ID_i, D_i, E_i, T_i\}$  and sends it to the server  $S$ . Meanwhile, in Step 4 of the authentication phase, the server  $S$  puts the timestamp  $T_s$  into the mutual authentication message  $\{F_i, G_i, T_s\}$  and conveys it to the user  $U_i$ . Therefore, the user  $U_i$  and the server  $S$  can verify the occurrence of a replay attack by checking timestamps  $T_i$  and  $T_s$ .

#### 5.1.7 Providing Perfect Forward Secrecy

Perfect forward secrecy can ensure that any previously established session keys are not disclosed to the attacker even if the server's master secret key is compromised. In our proposed scheme, the shared session key  $sk = h(\alpha \parallel \beta' \parallel h(A_i' \oplus ID_i)) = h(\alpha' \parallel \beta \parallel h(A_i \oplus ID_i))$ , where  $\alpha = \alpha'$ ,  $\beta = \beta'$ ,  $A_i = h(ID_i \oplus x) \parallel h(x)$  and  $A_i' = B_i \oplus h(r \parallel PW_i)$ . Suppose that an attacker obtained the server's master secret key  $x$ . If the attacker wants to derive the previous session key  $sk$ , they must know  $\alpha$

Table 2: Functionality comparison of our scheme and other related schemes

	F1	F2	F3	F4	F5	F6	F7	F8
Juang et al. [6]	Yes	Yes	Yes	Yes	Yes	Yes	No	Yes
Song [14]	Yes	Yes	Yes	Yes	No	Yes	No	Yes
Chen et al. [2]	Yes	Yes	Yes	Yes	No	Yes	No	Yes
Li et al. [9]	Yes	Yes	Yes	No	No	Yes	Yes	Yes
Sun et al. [17]	Yes	Yes	No	Yes	Yes	Yes	Yes	Yes
Li et al. [10]	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Our scheme	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes

F1: Mutual authentication; F2: Session key agreement; F3: Freely chosen and exchanged password; F4: Withstanding man in the middle attack; F5: Withstanding insider attack; F6: Withstanding replay attack; F7: Providing perfect forward secrecy; F8: Satisfying known-key security.

and  $\beta$ . However,  $\alpha$  and  $\beta$  are not directly transmitted between user  $U_i$  and server  $S$  via the public channel, but are encrypted into the ciphertext  $D_i$  and  $F_i$ , respectively. Therefore,  $\alpha$  and  $\beta$  cannot be obtained by the attacker, which implies that our proposed scheme provides perfect forward secrecy.

### 5.1.8 Satisfying Known-key Security

Known-key security guarantees that other session keys will not be derived by the attacker from the compromised session key. Our proposed scheme can satisfy known-key security by allowing user  $U_i$  and the server  $S$  to establish unique session keys in their different login and authentication phases. Assume that a session key  $sk = h(\alpha \parallel \beta \parallel h(A_i \oplus ID_i))$  is compromised. Since  $\alpha$  and  $\beta$  are random numbers selected by the user  $U_i$  and the server  $S$ , respectively, different values of  $\alpha$  and  $\beta$  will be selected in different sessions. As a result, even if the attacker gets  $sk$ ,  $\alpha$ , and  $\beta$ , they cannot compute another session key  $sk'$  from the compromised  $sk$  without knowing  $\alpha'$  and  $\beta'$  from the other sessions. Therefore, our proposed scheme can satisfy the known-key security problem.

The functionality comparison of our proposed scheme with other related works [2, 6, 9, 10, 14, 17] is summarized in Table 2, which infers that our proposed scheme is more secure and practical than other related works.

## 5.2 Performance Analysis

In this subsection, we evaluate the performance of our proposed scheme in terms of computational cost. Table 3 compares the computational cost of our proposed scheme and other related schemes [2, 6, 9, 10, 14, 17]. From Table 3, we can see that all of other existing schemes involve some time-consuming operations, such as modulus exponential operations, symmetric encryption/decryption operations or multiplication/division operations. In particular, among these three operations,

multiplication/division operations are faster than symmetric encryption/decryption operations while symmetric encryption/decryption operations are faster than modulus exponential operations. Fortunately, our proposed scheme only utilizes one-way hash functions, which are much faster than the mentioned three operations. Therefore, this method can significantly enhance computational efficiency while retaining higher security as shown in Table 2.

## 6 Conclusions

In this paper, we proposed a smart card based password authentication scheme to overcome the security weaknesses of Li et al.'s scheme. Our proposed scheme can achieve mutual authentication and users can freely choose and change their passwords. We prove that our proposed scheme can resist various types of attack, such as a man-in-the-middle attack, insider attack, and replay attack. Furthermore, our proposed scheme has better computational efficiency than other related works.

## References

- [1] C. C. Chang, C. Y. Lee and Y. C. Chiu, "Enhanced authentication scheme with anonymity for roaming service in global mobility networks," *Computer Communications*, vol. 32, no. 4, pp. 611–618, 2009.
- [2] B. L. Chen, W. C. Kuo and L. C. Wu, "Robust smart-card-based remote user password authentication scheme," *International Journal of Communication Systems*, in press. (<http://dx.doi.org/10.1002/dac.2368>)
- [3] T. ElGamal, "A public-key cryptosystem and a signature scheme based on discrete logarithms," *IEEE Transactions on Information Theory*, vol. 31, no. 4, pp. 469–472, 1985.
- [4] M. S. Hwang and L. H. Li, "A new remote user authentication scheme using smart card," *IEEE Trans-*



Table 3: Computational cost comparison of our scheme and other related schemes

	C1	C2	C3	C4	C5	C6
Juang et al. [6]	1H	2H+3S	3H+3S	4H+6S+1M	1H+5S	1H+5S
Song [14]	-	2H+E	3H+1S	3H+1S+1E	Null	Null
Chen et al. [2]	-	1H+1E	2H+2M+4E	H+M+4E	3H+2M+2E	3H+2M+3E
Li et al. [9]	-	2H+2E	4H+M+4E	3H+3E	3H+2M+4E	-
Sun et al. [17]	-	2H+1S	4H+2M	4H+1S+2M	2H	-
Li et al. [10]	1H	2H+3S	8H+4S	10H+10S+1M	1H+6S	1H+9S
Our scheme	1H	3H	6H	6H	4H	-

C1: Computational cost of the user in registration phase; C2: Computational cost of the server in registration phase; C3: Computational cost of the user in login and authentication phases; C4: Computational cost of the server in login and authentication phases; C5: Computational cost of the user in password change phase; C6: Computational cost of the server in password change phase; H: Hashing operation; E: Modulus exponential operation; S: Symmetric encryption/decryption operation; M: Multiplication/division operation; Null: Cannot provide this functionality.

actions on Consumer Electronics, vol. 46, no. 1, pp. 28–30, 2000.

- [5] W. S. Juang, “Efficient multi-server password authenticated key agreement using smart cards,” *IEEE Transactions on Consumer Electronics*, vol. 50, no. 1, pp. 251–255, 2004.
- [6] W. S. Juang, S. T. Chen and H. T. Liaw, “Robust and efficient password-authenticated key agreement using smart card,” *IEEE Transactions on Industrial Electronics*, vol. 55, no. 6, pp. 2551–2556, 2008.
- [7] S. K. Kim and M. G. Chung, “More secure remote user authentication scheme,” *Computer Communications*, vol. 32, no. 6, pp. 1018–1021, 2009.
- [8] L. Lamport, “Password authentication with insecure communication,” *Communications of the ACM*, vol. 24, no. 11, pp. 770–772, 1981.
- [9] X. Li, J. Niu, M. K. Khan, and J. Liao, “An enhanced smart card based remote user password authentication scheme,” *Journal of Network and Computer Applications*, in press. (<http://dx.doi.org/10.1016/j.jnca.2013.02.034>.)
- [10] X. X. Li, W. D. Qiu, D. Zheng, K. F. Chen, and J. H. Li, “Anonymity enhancement on robust and efficient password-authenticated key agreement using smart cards,” *IEEE Transactions on Industrial Electronics*, vol. 57, no. 2, pp. 793–800, 2010.
- [11] J. Y. Liu, A. M. Zhou, and M. X. Gao, “A new mutual authentication scheme based on nonce and smart card,” *Computer Communications*, vol. 31, no. 10, pp. 2205–2209, 2008.
- [12] M. Peyravian and N. Zunic, “Methods for protecting password transmission,” *Computer and Security*, vol. 19, no. 5, pp. 466–469, 2006.
- [13] B. Schneier, *Applied Cryptography (2nd Edition)*, New York: Wiley, 1996.
- [14] R. Song, “Advanced smart card based password authentication protocol,” *Computer Standards and Interfaces*, vol. 32, no. 5, pp. 321–325, 2010.
- [15] S. K. Sood, A. K. Sarje, and K. Singh, “An improvement of xu et al.’s authentication scheme using smart cards,” in *Proceedings of the Third Annual ACM Bangalore Conference*, pp. 17–22, Bangalore, Karnataka, India, 2010.
- [16] D. Z. Sun, J. P. Huai, J. Z. Sun, and J. X. Li, “Cryptanalysis of a mutual authentication scheme based on nonce and smart cards,” *Computer Communications*, vol. 32, no. 6, pp. 1015–1017, 2009.
- [17] D. Z. Sun, J. P. Huai, J. Z. Sun, J. X. Li, J. W. Zhang, and Z. Y. Feng, “Improvements of juang et al.’s password-authenticated key agreement scheme using smart cards,” *IEEE Transactions on Industrial Electronics*, vol. 56, no. 6, pp. 2284–2291, 2009.
- [18] H. M. Sun, “An efficient remote user authentication scheme using smart cards,” *IEEE Transactions on Consumer Electronics*, vol. 46, no. 4, pp. 958–961, 2000.
- [19] T. C. Wu and H. S. Sung, “Authentication passwords over an insecure channel,” *Computer and Security*, vol. 15, no. 5, pp. 431–439, 1996.
- [20] J. Xu, W. T. Zhu, and D. G. Feng, “An improved smart card based password authentication scheme with provable security,” *Computer Standards and Interfaces*, vol. 31, no. 4, pp. 723–728, 2009.

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