Compositional Deep Learning



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Workshop on Vector Space Modeling for NLP 2015



From symbolic to distributed representations

The vast majority of rule-based and statistical NLP work regarded words as atomic symbols: hotel, conference, walk

In vector space terms, this is a vector with one 1 and a lot of zeroes

We call this a "one-hot" representation.

Its problem:

```
motel [000000000010000]^T
hotel [00000001000000] = 0
```



Distributional similarity based representations

You can get a lot of value by representing a word by means of its neighbors

"You shall know a word by the company it keeps"

(J. R. Firth 1957: 11)

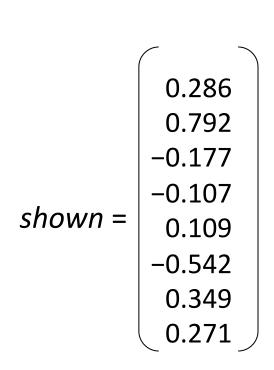
One of the most successful ideas of modern NLP

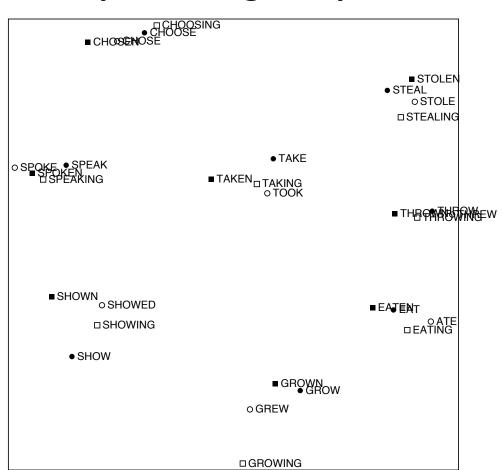
government debt problems turning into banking crises as has happened in saying that Europe needs unified banking regulation to replace the hodgepodge

These words will represent banking 7



With distributed, distributional representations, syntactic and semantic patterning is captured





[Rohde et al. 2005. An Improved Model of Semantic Similarity Based on Lexical Co-Occurrence]



- 1. Vector space representations of language
- 2. Predict! vs. Count!: The GloVe model of word vectors

- 3. Wanted: meaning composition functions
- 4. Tree-structured Recursive Neural Networks for Semantics
- 5. Natural Language Inference with TreeRNNs



LSA vs. word2vec

LSA: Count!

- Factorize a (maybe weighted, maybe log scaled) termdocument or word-context matrix (Schütze 1992) into $U\Sigma V^T$
- Retain only k singular values, in order to generalize

$$\begin{bmatrix}
* & * & * & * & * \\
* & * & * & * & * \\
* & * & * & * & *
\end{bmatrix} = \begin{bmatrix}
\star & \star & \star \\
\star & \star & \star
\end{bmatrix}$$

$$\begin{bmatrix}
* & \star & \star & \star & \star \\
\star & \star & \star & \star
\end{bmatrix}$$

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$$\begin{bmatrix}
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\star & \star & \star & \star
\end{bmatrix}$$

[Cf. Baroni: Don't count, predict! A systematic comparison of context-counting vs. context-predicting semantic vectors. ACL 2014]



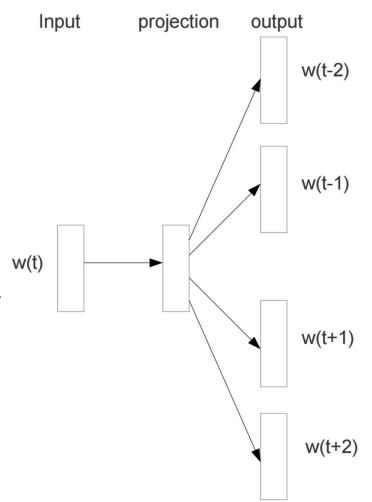


LSA vs. word2vec

LSA: Count! vs.

word2vec CBOW/SkipGram: Predict!

- Train word vectors to try to either:
 - Predict a word given its bag-ofwords context (CBOW); or
 - Predict a context word (positionindependent) from the center word
- Update word vectors until they can do this prediction well





Word Analogies: word2vec captures dimensions of similarity as linear relations

Test for linear relationships, examined by Mikolov et al. 2013

a:b::c:?
$$d = \arg\max_{x} \frac{(w_b - w_a + w_c)^T w_x}{||w_b - w_a + w_c||}$$

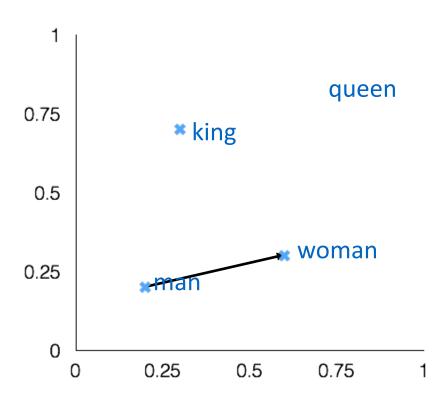
man:woman :: king:?



- man [0.20 0.20]

woman [0.60 0.30]

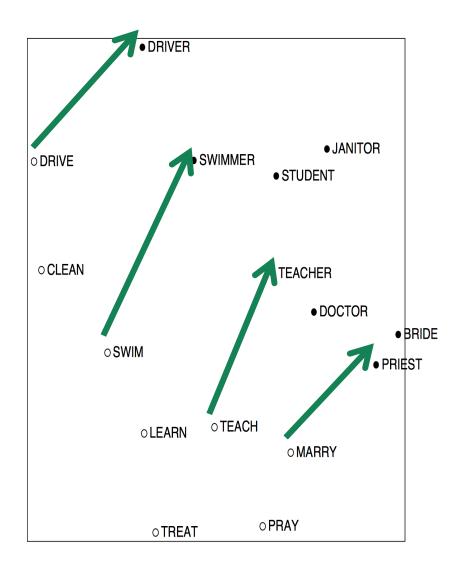
queen [0.70 0.80]





COALS model (count-modified LSA)

[Rohde, Gonnerman & Plaut, ms., 2005]





Count based vs. direct prediction

LSA, HAL (Lund & Burgess),
COALS (Rohde et al),
Hellinger-PCA (Lebret & Collobert)

- Fast training
- Efficient usage of statistics
- Primarily used to capture word similarity
- Disproportionate importance given to small counts

• NNLM, HLBL, RNN, word2vec Skip-gram/CBOW, (Bengio et al; Collobert & Weston; Huang et al; Mnih & Hinton; Mikolov et al; Mnih & Kavukcuoglu)

- Scales with corpus size
- Inefficient usage of statistics
- Generate improved performance on other tasks
- Can capture complex patterns beyond word similarity



Encoding meaning in vector differences

[Pennington, Socher, and Manning, EMNLP 2014]

Crucial insight: Ratios of co-occurrence probabilities can encode meaning components

	x = solid	x = gas	x = water	x = random
P(x ice)	large	small	large	small
P(x steam)	small	large	large	small
$\frac{P(x \text{ice})}{P(x \text{steam})}$	large	small	~1	~1



Encoding meaning in vector differences

[Pennington, Socher, and Manning, EMNLP 2014]

Crucial insight: Ratios of co-occurrence probabilities can encode meaning components

	x = solid	x = gas	x = water	x = fashion
P(x ice)	1.9 x	6.6 x	3.0 x	1.7 x
	10 ⁻⁴	10 ⁻⁵	10 ⁻³	10 ⁻⁵
P(x steam)	2.2 x	7.8 x	2.2 x	1.8 x
	10 ⁻⁵	10 ⁻⁴	10 ⁻³	10 ⁻⁵
$\frac{P(x \text{ice})}{P(x \text{steam})}$	8.9	8.5 x 10 ⁻²	1.36	0.96



Encoding meaning in vector differences

Q: How can we capture ratios of co-occurrence probabilities as meaning components in a word vector space?

A: Log-bilinear model:
$$w_i \cdot w_j = \log P(i|j)$$

with vector differences
$$w_x \cdot (w_a - w_b) = \log rac{P(x|a)}{P(x|b)}$$



GloVe: A new model for learning word representations [Pennington et al., EMNLP 2014]



$$w_i \cdot w_j = \log P(i|j)$$

$$w_x \cdot (w_a - w_b) = \log \frac{P(x|a)}{P(x|b)}$$

$$J = \sum_{i,j=1}^{V} f(X_{ij}) \left(w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log X_{ij} \right)^2 \qquad f \sim \begin{bmatrix} 1.0 \\ 0.8 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.0 \end{bmatrix}$$



Word similarities

Nearest words to frog:

- 1. frogs
- 2. toad
- 3. litoria
- 4. leptodactylidae
- 5. rana
- 6. lizard
- 7. eleutherodactylus



litoria



leptodactylidae



rana



eleutherodactylus

http://nlp.stanford.edu/projects/glove/



Word Analogies [Mikolov et al., 2012, 2013]

Task: predict the last column

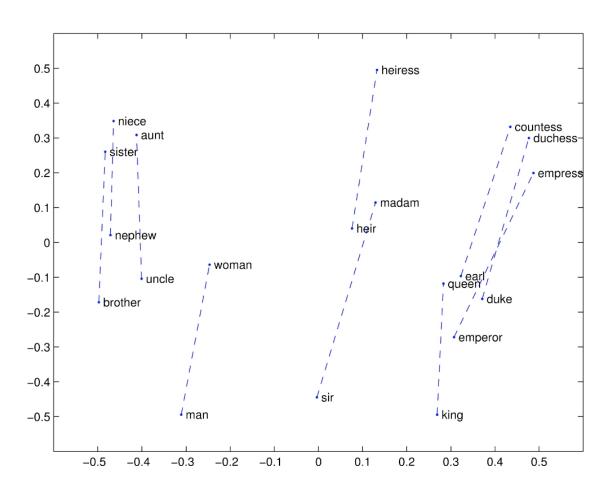
Type of relationship	Word Pair 1		Word Pair 2	
Common capital city	Athens	Greece	Oslo	Norway
All capital cities	Astana	Kazakhstan	Harare	Zimbabwe
Currency	Angola	kwanza	Iran	rial
City-in-state	Chicago	Illinois	Stockton	California
Man-Woman	brother	sister	grandson	granddaughter
Adjective to adverb	apparent	apparently	rapid	rapidly
Opposite	possibly	impossibly	ethical	unethical
Comparative	great	greater	tough	tougher
Superlative	easy	easiest	lucky	luckiest
Present Participle	think	thinking	read	reading
Nationality adjective	Switzerland	Swiss	Cambodia	Cambodian
Past tense	walking	walked	swimming	swam
Plural nouns	mouse	mice	dollar	dollars
Plural verbs	work	works	speak	speaks



Model	Dimensions	Corpus size	Performance (Syn + Sem)
CBOW (Mikolov et al. 2013b)	300	1.6 billion	36.1



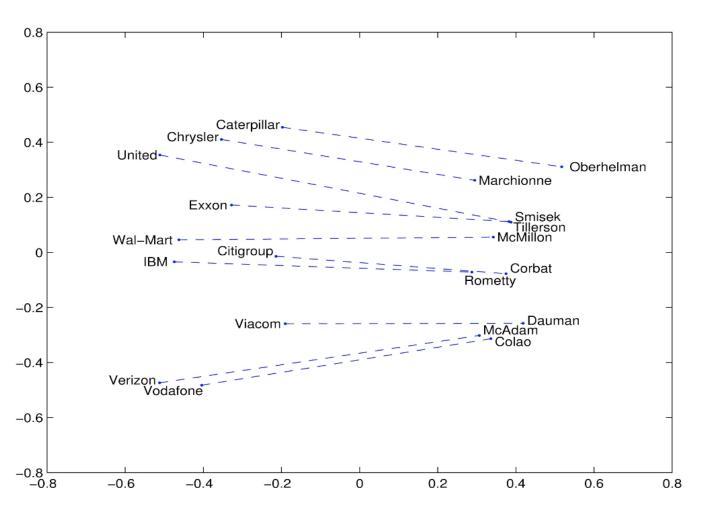
Glove Visualizations



http://nlp.stanford.edu/projects/glove/

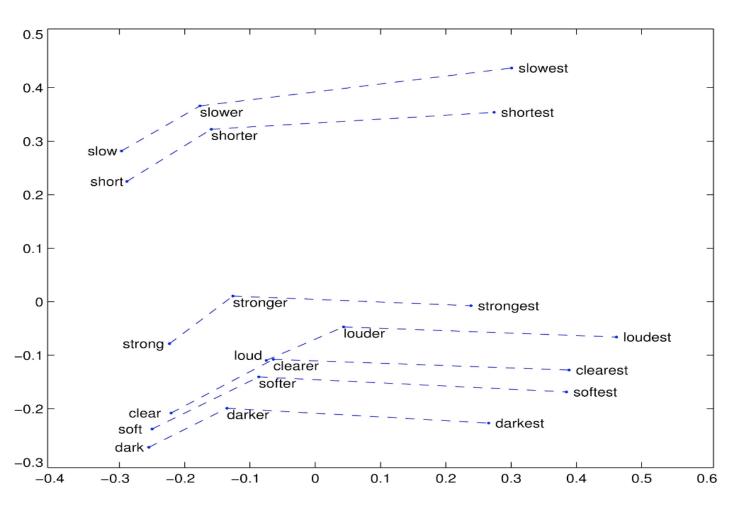


Glove Visualizations: Company - CEO



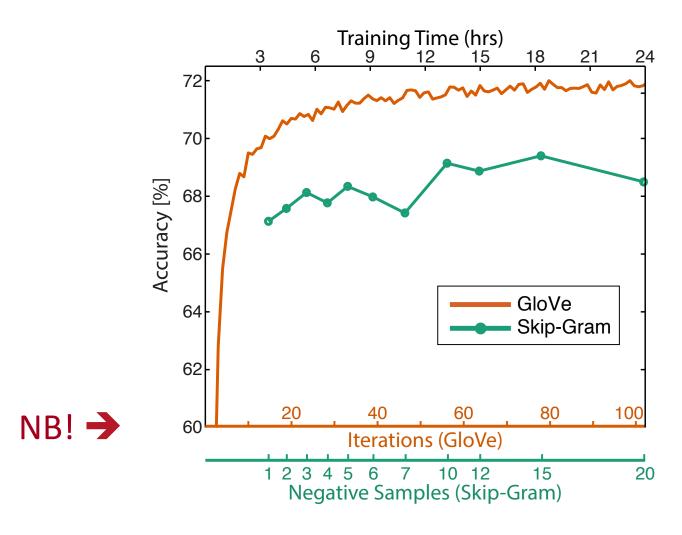


Glove Visualizations: Superlatives



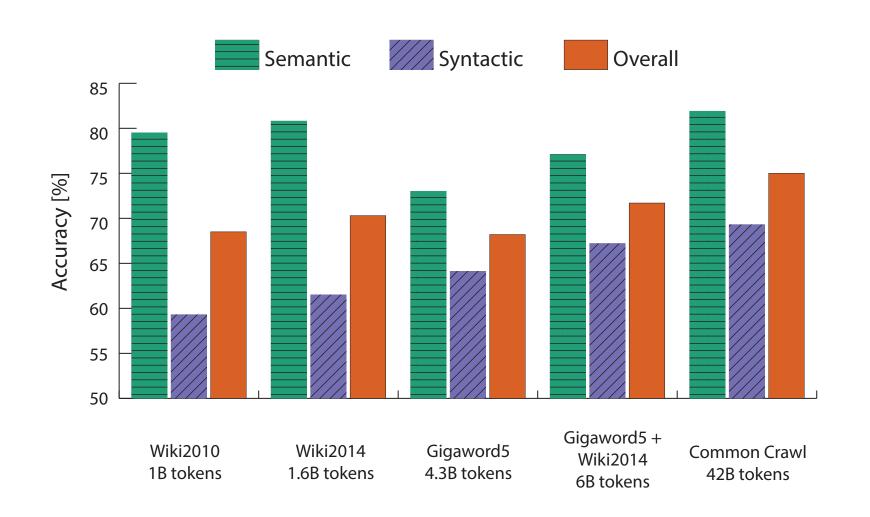


Analogy evaluation and hyperparameters





Analogy evaluation and hyperparameters





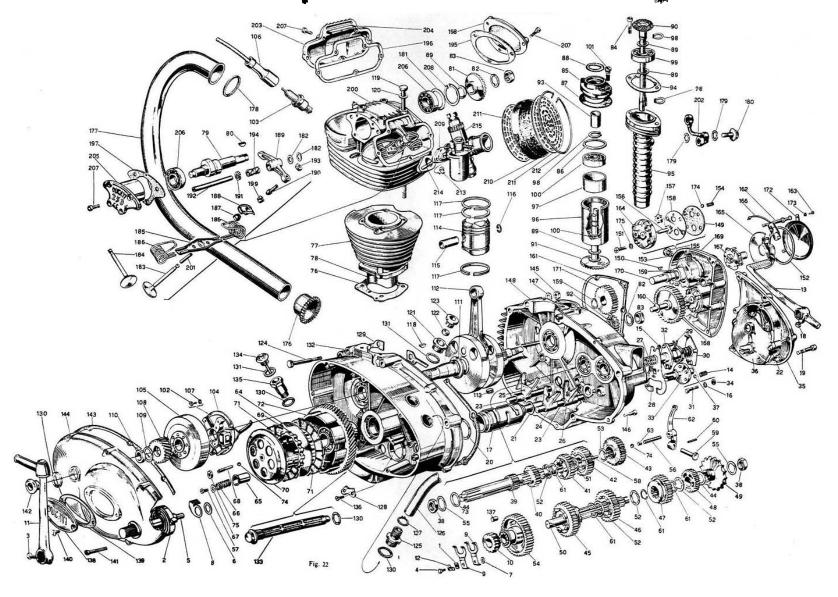
Word Embeddings Conclusion

We developed a model that can translate meaningful relationships between word-word co-occurrence probabilities into linear relations in the word vector space

GloVe shows the connection between **Count!** work and **Predict!** work – appropriate scaling of counts gives the properties and performance of **Predict!** models

Can one **explain** word2vec's linear structure? See Arora, Li, Liang, Ma, & Risteski. 2015. Random Walks on Context Spaces: Towards an Explanation of the Mysteries of Semantic Word Embeddings. [Develops a generative model.]

Compositionality



Artificial Intelligence requires understanding bigger things from knowing about smaller things



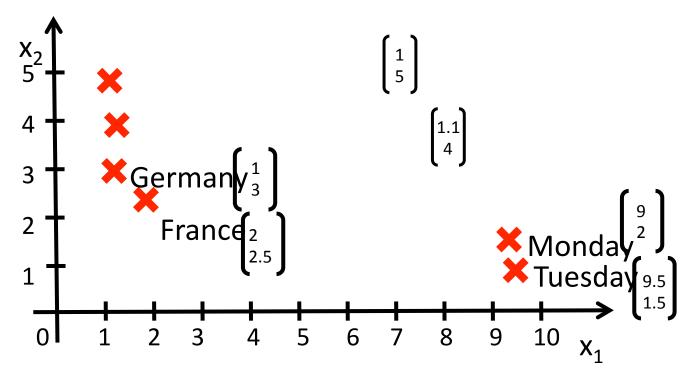
WE need more! What of larger semantic units?

How can we know when larger units are similar in meaning?

- Two senators received contributions engineered by lobbyist Jack Abramoff in return for political favors.
- Jack Abramoff attempted to bribe two legislators.

People interpret the meaning of larger text units — entities, descriptive terms, facts, arguments, stories — by semantic composition of smaller elements

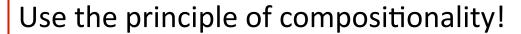
Representing Phrases as Vectors



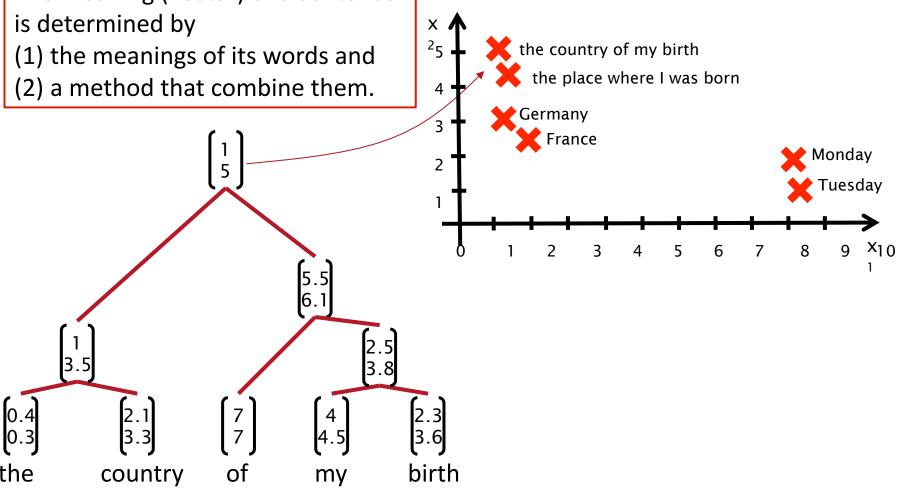
Vector for single words are useful as features but limited! the country of my birth the place where I was born

Can we extend the ideas of word vector spaces to phrases?

How should we map phrases into a vector space?



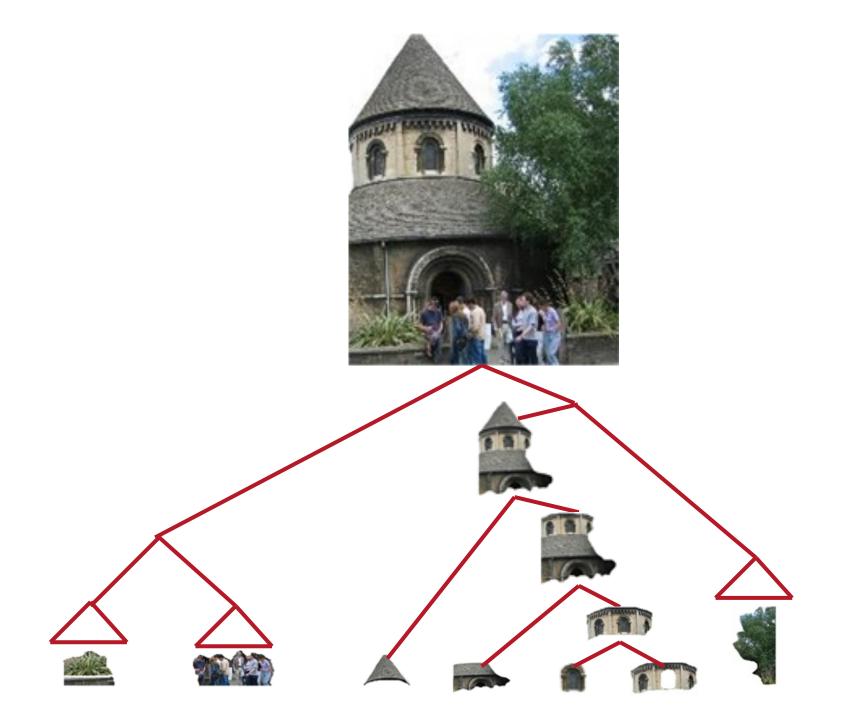
The meaning (vector) of a sentence is determined by



$$e^{-}(x-\mu)^2$$
 $2\sigma^2$

$$\Phi(x) = \sqrt{\frac{1}{\tau \sigma}} e^{\frac{-(x-x)^2}{2\sigma^2}}$$

$$\frac{1}{\sqrt{2\pi\sigma}}$$
 $e^{\frac{(x-\mu)^2}{2\sigma^2}}$



Can we build meaning composition functions in deep learning systems?

Word2vec is the sriracha sauce of deep learning!



Coren @coren42



Obvious trend at #naacl2015: Embeddings are now so hip that hipsters are moving away from embeddings.

6/3/15, 4:50 PM

2 FAVORITES



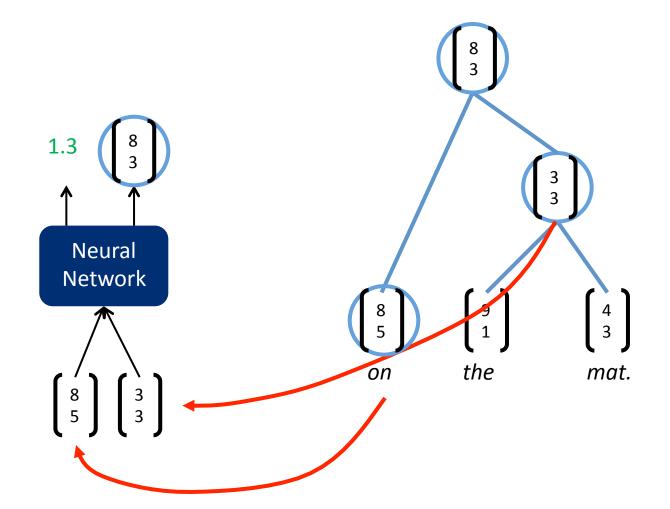






Tree Recursive Neural Networks (Tree RNNs)

Basic computational unit: Recursive Neural Network (Goller & Küchler 1996, Costa et al. 2003, Socher et al. ICML, 2011)



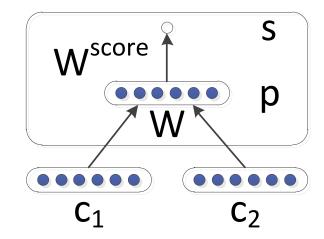
Version 1: Simple concatenation Tree RNN

$$p = \tanh(W \begin{bmatrix} c_1 \\ c_2 \end{bmatrix} + b),$$

where tanh:



score =
$$V^T p$$



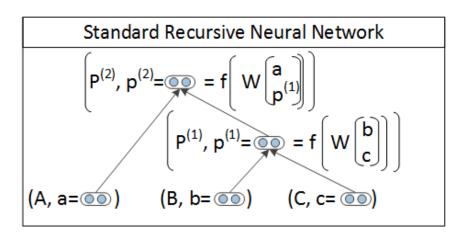
Only a single weight matrix = composition function!

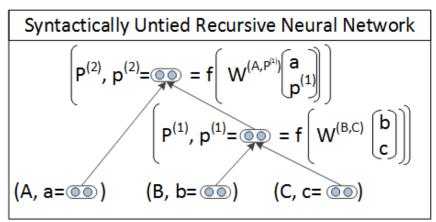
No really interaction between the input words!

Not adequate for human language composition function

Version 2: PCFG + Syntactically-Untied RNN

- A symbolic Context-Free Grammar (CFG) backbone is adequate for basic syntactic structure
- We use the discrete syntactic categories of the children to choose the composition matrix
- An RNN can do better with a different composition matrix for different syntactic environments
- The result gives us a better semantics

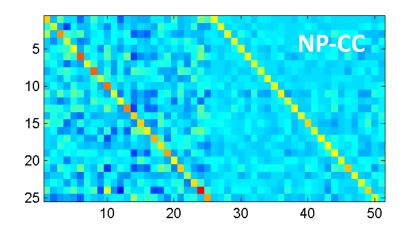


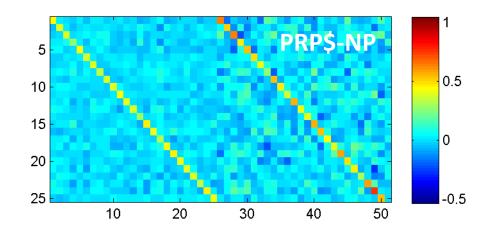


SU-RNN

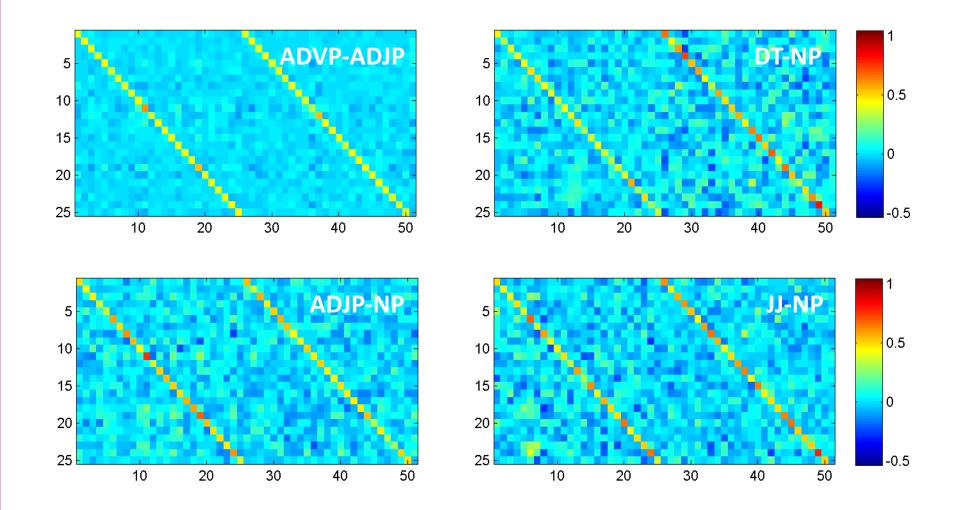
Learns soft notion of head words

Initialization:
$$W^{(\cdot \cdot)} = 0.5[I_{n \times n}I_{n \times n}0_{n \times 1}] + \epsilon$$





SU-RNN





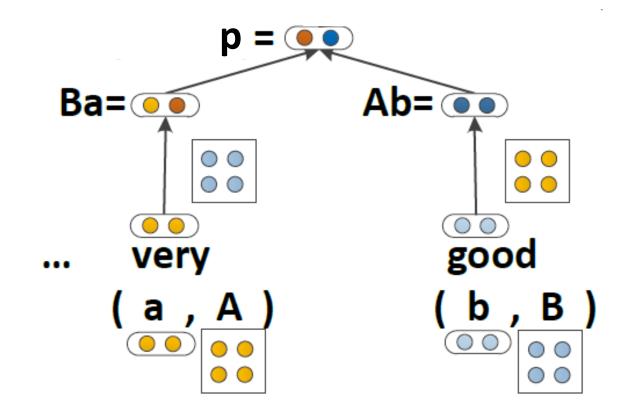
Version 3: Matrix-vector RNNs



[Socher, Huval, Bhat, Manning, & Ng, 2012]

$$p = f\left(W\left[\begin{array}{c} a \\ b \end{array}\right]\right)$$

$$p = f\left(W \left[\begin{array}{c} Ba \\ Ab \end{array}\right]\right)$$

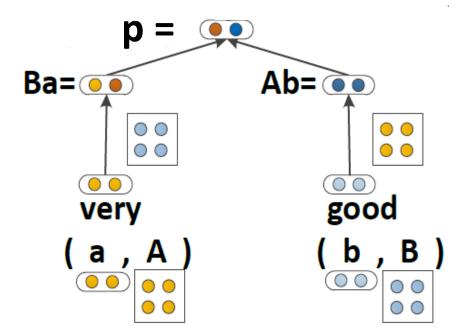




Version 3: Matrix-vector RNNs

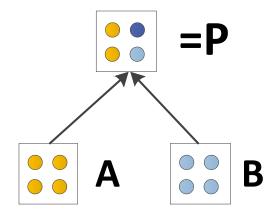
[Socher, Huval, Bhat, Manning, & Ng, 2012]

$$p = f\left(W\left[\begin{array}{c} Ba \\ Ab \end{array}\right]\right)$$



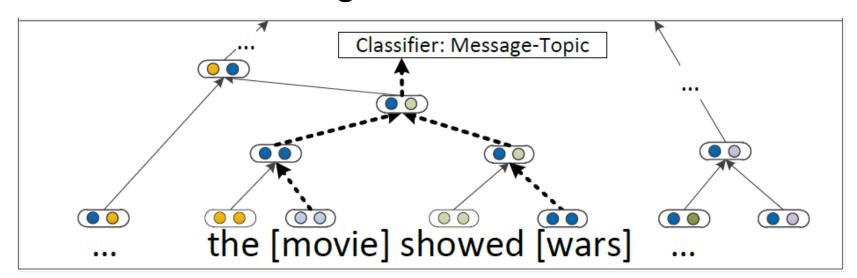
$$P = g(A, B) = W_M \left[\begin{array}{c} A \\ B \end{array} \right]$$

$$W_M \in \mathbb{R}^{n \times 2n}$$



Classification of Semantic Relationships

- Can an MV-RNN learn how a large syntactic context conveys a semantic relationship?
- My [apartment]_{e1} has a pretty large [kitchen]_{e2}
 → component-whole relationship (e2,e1)
- Build a single compositional semantics for the minimal constituent including both terms

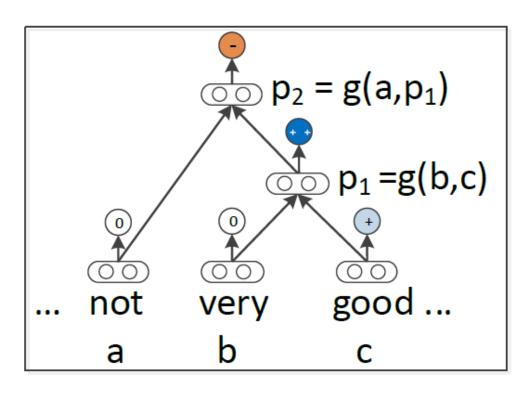


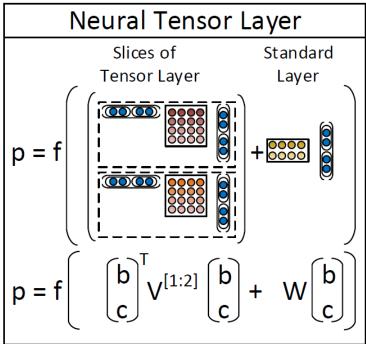
Classification of Semantic Relationships

Classifier	Features	F1
SVM	POS, stemming, syntactic patterns	60.1
MaxEnt	POS, WordNet, morphological features, noun compound system, thesauri, Google n-grams	77.6
SVM	POS, WordNet, prefixes, morphological features, dependency parse features, Levin classes, PropBank, FrameNet, NomLex-Plus, Google n-grams, paraphrases, TextRunner	82.2
RNN	_	74.8
MV-RNN	_	79.1
MV-RNN	POS, WordNet, NER	82.4

Version 4: Recursive Neural Tensor Network

- Less parameters than MV-RNN
- Allows the two word or phrase vectors to interact multiplicatively





Beyond the bag of words: Sentiment detection

Is the tone of a piece of text positive, negative, or neutral?

- Sentiment is that sentiment is "easy"
- Detection accuracy for longer documents ~90%, BUT

```
... ... loved ... ... ... great ... ... ... ... impressed ... ... ... marvelous ... ... ...
```

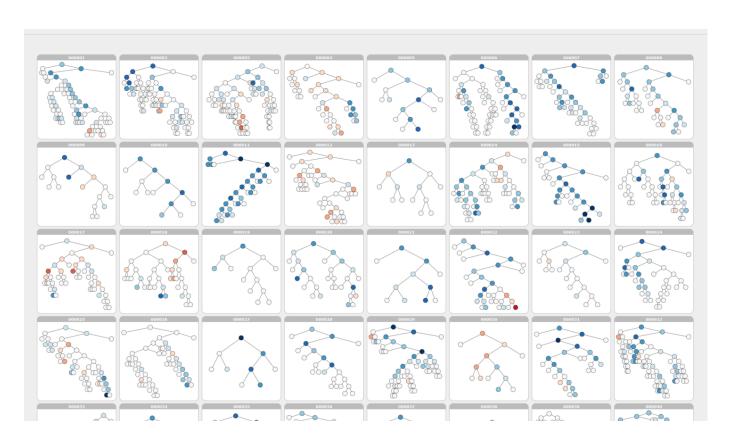


With this cast, and this subject matter, the movie should have been funnier and more entertaining.



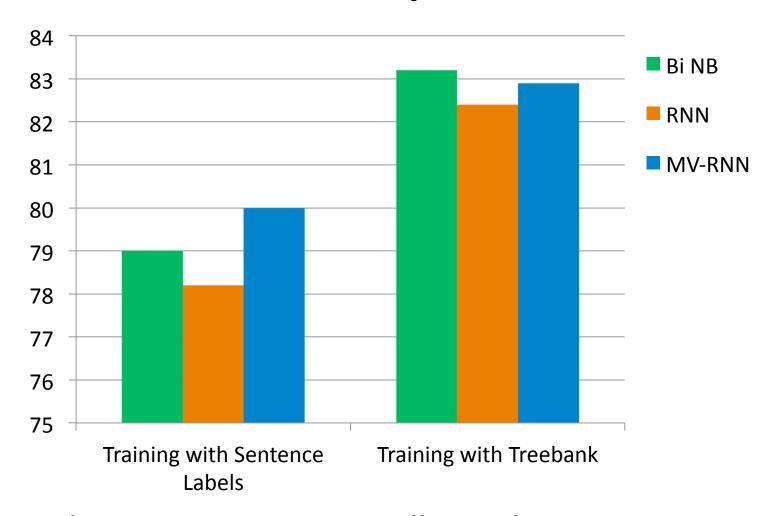
Stanford Sentiment Treebank

- 215,154 phrases labeled in 11,855 sentences
- Can actually train and test compositions



http://nlp.stanford.edu:8080/sentiment/

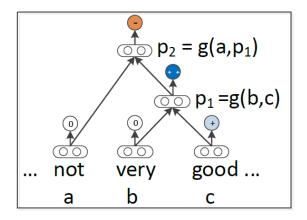
Better Dataset Helped All Models

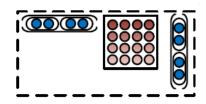


- Hard negation cases are still mostly incorrect
- We also need a more powerful model!

Version 4: Recursive Neural Tensor Network

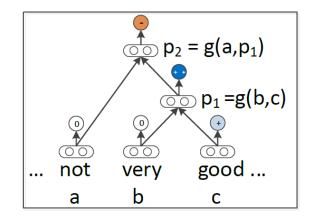
 Idea: Allow both additive and mediated multiplicative interactions of vectors

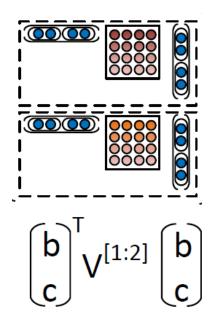




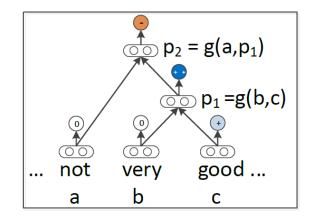
$$\begin{bmatrix} b \\ c \end{bmatrix}^T V \begin{bmatrix} b \\ c \end{bmatrix}$$

Recursive Neural Tensor Network





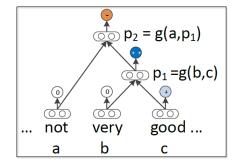
Recursive Neural Tensor Network

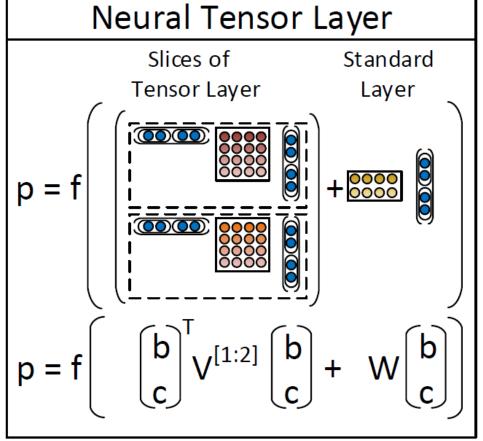


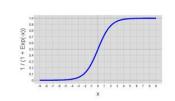
$$\begin{bmatrix} b \\ c \end{bmatrix}^{T} V^{[1:2]} \begin{bmatrix} b \\ c \end{bmatrix} + W \begin{bmatrix} b \\ c \end{bmatrix}$$

Recursive Neural Tensor Network

- Use resulting vectors in tree as input to a classifier like logistic regression
- Train all weights jointly with gradient descent

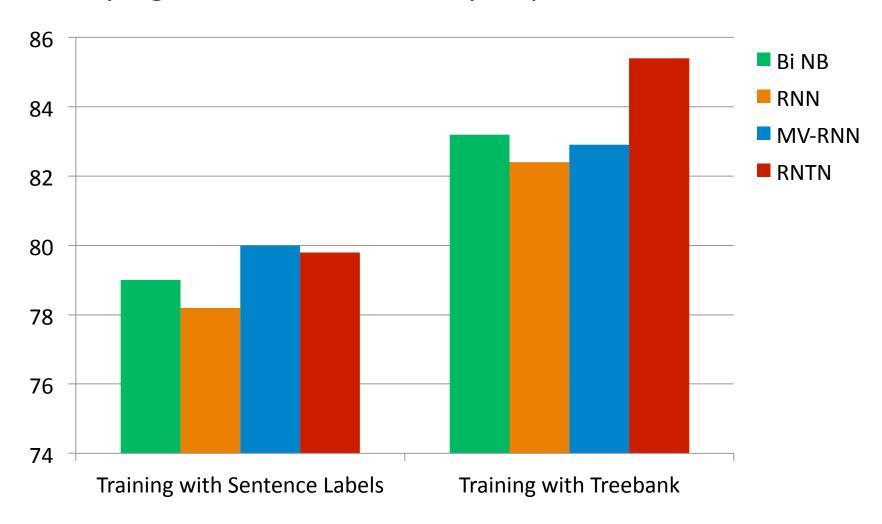






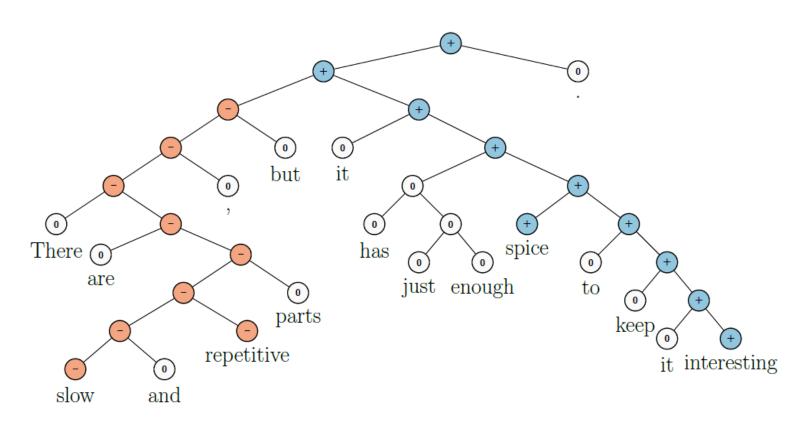
Positive/Negative Results on Treebank

Classifying Sentences: Accuracy improves to 85.4



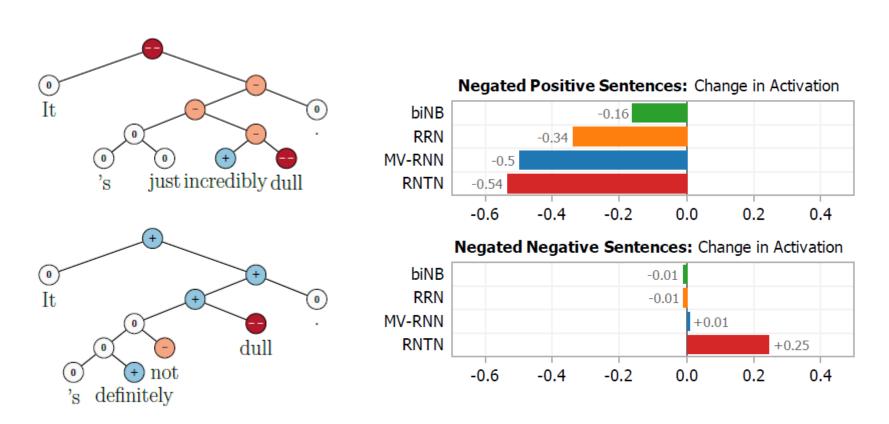
Experimental Results on Treebank

- RNTN can capture constructions like X but Y
- RNTN accuracy of 72%, compared to MV-RNN (65%), biword NB (58%) and RNN (54%)



Negation Results

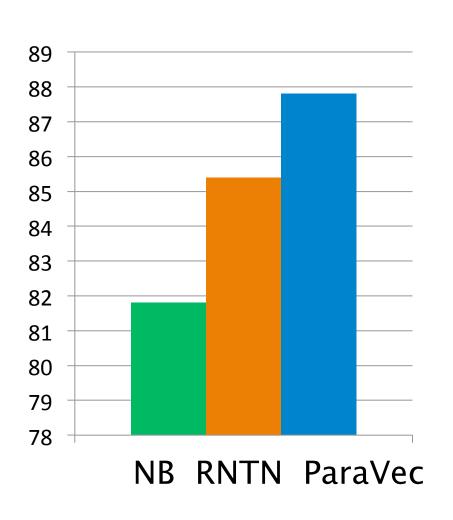
When negating negatives, positive activation should increase!

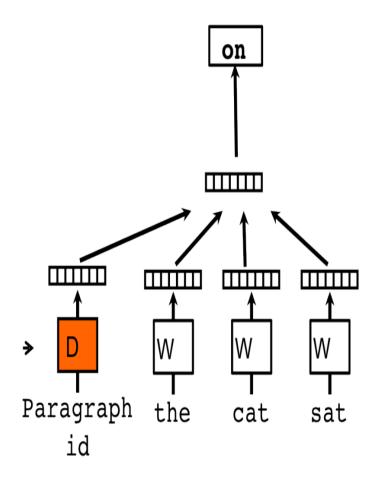


Demo: http://nlp.stanford.edu:8080/sentiment/

A disappointment

Beaten by a word2vec extension with no sentence structure!







Version 5: Improving Deep Learning Semantic Representations using a TreeLSTM



[Tai et al., ACL 2015]

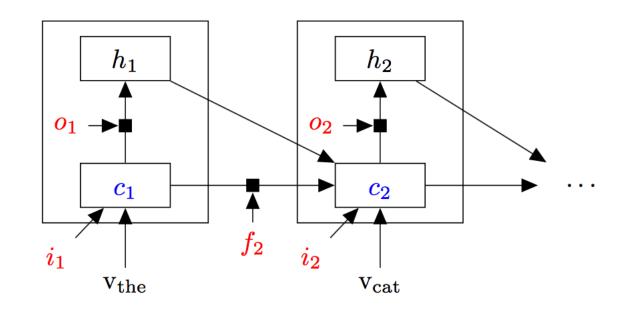
Goals:

- Still trying to represent the meaning of a sentence as a location in a (high-dimensional, continuous) vector space
- In a way that accurately handles semantic composition and sentence meaning
- Beat Paragraph Vector!

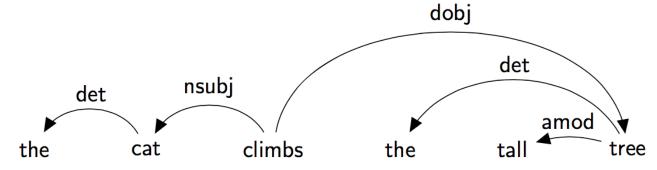


Tree-Structured Long Short-Term Memory Networks

Use Long Short-Term Memories (Hochreiter and Schmidhuber 1997)



Use syntactic structure

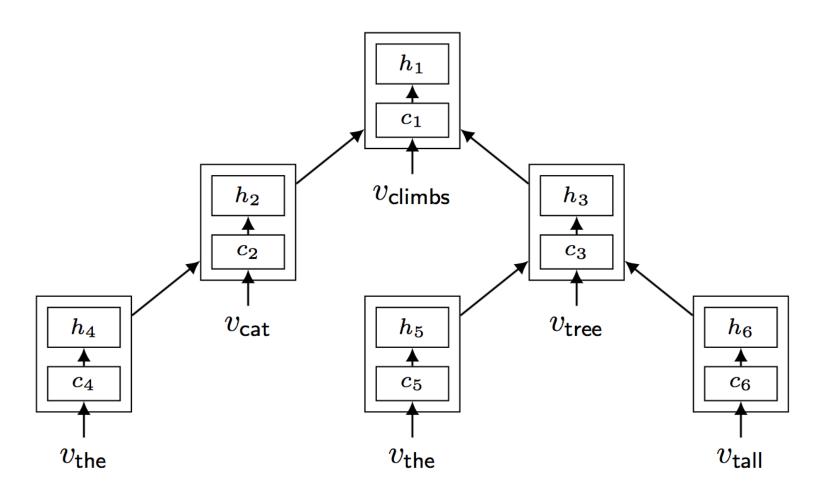




- An LSTM creates a sentence representation via left-to-right composition
- Natural language has syntactic structure
- We can use this additional structure over inputs to guide how representations should be composed



Tree-Structured Long Short-Term Memory Networks [Tai et al., ACL 2015]





Results: Sentiment Analysis: Stanford Sentiment Treebank

Method	Accuracy % (Fine-grain, 5 classes)
RNTN (Socher et al. 2013)	45.7
Paragraph-Vec (Le & Mikolov 2014)	48.7
DRNN (Irsoy & Cardie 2014)	49.8
Tree LSTM	50.9



Results: Semantic Relatedness

SICK 2014 (Sentences Involving Compositional Knowledge)

Method	Pearson correlation
Meaning Factory (Bjerva et al. 2014)	0.827
ECNU (Zhao et al. 2014)	0.841
LSTM (sequence model)	0.853
Tree LSTM	0.868



Natural Language Inference

Can we tell if one piece of text follows from another?

- Two senators received contributions engineered by lobbyist Jack Abramoff in return for political favors.
- Jack Abramoff attempted to bribe two legislators.

Natural Language Inference = Recognizing Textual Entailment [Dagan 2005, MacCartney & Manning, 2009]



The task: Natural language inference

James Byron Dean refused to move without blue jeans

{entails, contradicts, neither}

James Dean didn't dance without pants



MacCartney's natural logic

An implementable logic for natural language inference without logical forms. (MacCartney and Manning '09)

Sound logical interpretation (lcard and Moss '13)

P	James Dean	refused to			move	without	blue	jeans
Н	James Byron Dean		did	n't	dance	without		pants
edit index	ı	2	3	4	5	6	7	8
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The task: Natural language inference

Claim: Simple task to define, but engages the full complexity of compositional semantics:

- Lexical entailment
- Quantification
- Coreference
- Lexical/scope ambiguity
- Commonsense knowledge
- Propositional attitudes
- Modality
- Factivity and implicativity

...



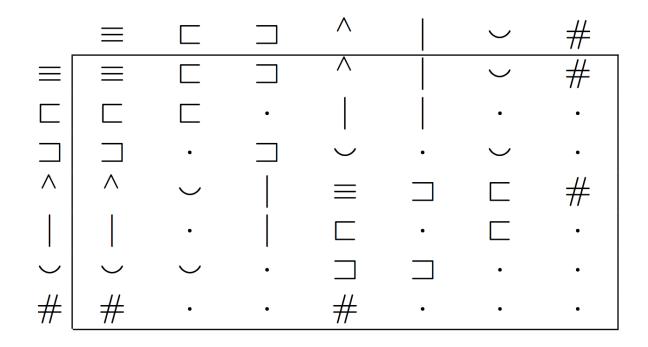
Natural logic: relations

Seven possible relations between phrases/sentences:

<i>x</i> ≡ <i>y</i>	equivalence	couch ≡ sofa
<i>x</i> □ <i>y</i>	forward entailment (strict)	crow □ bird
<i>x</i> ⊐ <i>y</i>	reverse entailment (strict)	European ⊐ French
x ^ y	negation (exhaustive exclusion)	human ^ nonhuman
x y	alternation (non-exhaustive exclusion)	cat dog
<i>x</i> _ <i>y</i>	COVEr (exhaustive non-exclusion)	animal nonhuman
<i>x</i> # <i>y</i>	independence	hungry # hippo



Natural logic: relation joins



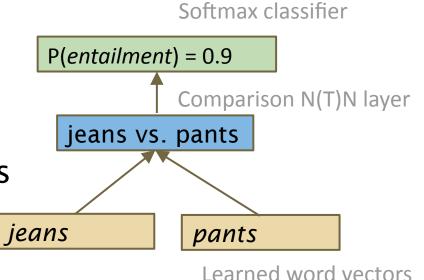
Can our NNs learn to make these inferences over pairs of embedding vectors?



A minimal NN for lexical relations [Bowman 2014]



- Words are learned embedding vectors.
- One plain TreeRNN or TreeRNTN layer
- Softmax emits relation labels
- Learn everything with SGD.





Lexical relations: results

	Train	Test	
# only	53.8 (10.5)	53.8 (10.5)	
15d NN	99.8 (99.0)	94.0 (87.0)	
15d NTN	100 (100)	99.6 (95.5)	

- Both models tuned, then trained to convergence on five randomly generated datasets
- Reported figures: % correct (macroaveraged F1)
- Both NNs used 15d embeddings, 75d comparison layer



Experimental paradigm: Train on relational statements generated from some formal system, test on other such relational statements.

The model needs to:

- Learn the relations between individual words. (lexical relations)
- Learn how lexical relations impact phrasal relations.
 (projectivity)
- Quantifiers present some of the harder cases of both of these.



Quantifiers

- Small vocabulary
 - Three basic types:
 - Quantifiers: some, all, no, most, two, three, not-all, not-most, less-than-two, less-than-three
 - Predicates: dog, cat, mammal, animal ...
 - Negation: not
- 60k examples generated using a generative implementation of the relevant portion of MacCartney and Manning's logic.
- All sentences of the form QPP, with optional negation on each predicate.

```
(most warthogs) walk
(most mammals) move
(most (not pets)) (not swim)

^ (not-most warthogs) walk
(not-most (not turtles)) move
(not-most (not pets)) move
```



Quantifier results

	Train	Test
Most freq. class (# only)	35.4%	35.4%
25d SumNN (sum of words)	96.9%	93.9%
25d TreeRNN	99.6%	99.2%
25d TreeRNTN	100%	99.7%



Natural language inference data

[Bowman, Manning & Potts 2015]

- To do NLI on real English, we need to teach an NN model English almost from scratch.
- What data do we have to work with:
 - GloVe/word2vec (useful w/ any data source)
 - SICK: Thousands of examples created by editing and pairing hundreds of sentences.
 - RTE: Hundreds of examples created by hand.
 - DenotationGraph: Millions of extremely noisy examples (~73% correct?) constructed fully automatically.



Results on SICK (+DG, +tricks) so far

	SICK Train	DG Train	Test
Most freq. class	56.7%	50.0%	56.7%
30 dim TreeRNN	95.4%	67.0%	74.9%
50 dim TreeRNTN	97.8%	74.0%	76.9%



Are we competitive? Sort of...

Best result (UIllinois) 84.5%

≈ interannotator agreement!

Median submission (out of 18): 77%

Our TreeRNTN: 76.9%

We're a purely-learned system

None of the ones in the competition were



Natural language inference data

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 - Stanford NLI corpus: ~600k examples, written by Turkers.



The Stanford NLI corpus

Instructions

The Stanford University NLP Group is collecting data for use in research on computer understanding of English. We appreciate your help!

We will show you the caption for a photo. We will not show you the photo. Using only the caption and what you know about the world:

- Write one alternate caption that is definitely a true description of the photo.
- Write one alternate caption that might be a true description of the photo.
- Write one alternate caption that is definitely an false description of the photo.

Photo caption A little boy in an apron helps his mother cook.

Definitely correct Example: For the caption "Two dogs are running through a field." you could write "There are animals outdoors."

Write a sentence that follows from the given caption.

Maybe correct Example: For the caption "Two dogs are running through a field." you could write "Some puppies are running to catch a stick."

Write a sentence which may be true given the caption, and may not be.

Definitely incorrect Example: For the caption "Two dogs are running through a field." you could write "The pets are sitting on a couch."

Write a sentence which contradicts the caption.

Problems (optional) If something is wrong with the caption that makes it difficult to understand, do your best above and let us know here.



There are very good reasons to want to represent meaning with distributed representations

So far, distributional learning has been most effective for this

But cf. [Young, Lai, Hodosh & Hockenmaier 2014] on denotational representations, using visual scenes

However, we want not just word meanings! We want:

Meanings of larger units, calculated compositionally

The ability to do natural language inference